

$$\sin^2 x - \sqrt{2}\cos(2x - \pi/4) = 1$$

$$\sin^2 x - \sqrt{2}(\cos 2x \cdot \cos \pi/4 + \sin 2x \cdot \sin \pi/4) = 1$$

$$\sin^2 x - \sqrt{2}(\cos 2x \cdot \sqrt{2}/2 + \sin 2x \cdot \sqrt{2}/2) = 1$$

$$\sin^2 x - \cos 2x - \sin 2x - 1 = 0$$

$$\sin^2 x - 2\cos^2(x) - 2\sin x \cdot \cos x = 0$$

$$\sin x = v$$

$$\cos x = u$$

Пусть $u=0 \Rightarrow v^2 - 2u^2 - 2uv = 0 \Rightarrow v=0 \Rightarrow u \neq 0$

$$v^2 - 2u^2 - 2uv = 0 | : u^2$$

$$v^2/u^2 - 2 - 2v/u = 0$$

$$v/u = t$$

$$t^2 - 2t - 2 = 0$$

$$D = 4 + 8 = 12$$

$$t_1 = (2 + \sqrt{12})/2 = 1 + \sqrt{3}$$

$$t_2 = (2 - \sqrt{12})/2 = 1 - \sqrt{3}$$

$$v/u = 1 + \sqrt{3}$$

$$\sin x / \cos x = 1 + \sqrt{3}$$

$$\operatorname{tg} x = 1 + \sqrt{3}$$

$$x = \operatorname{arctg}(1 + \sqrt{3}) + \pi k$$

$$x = \operatorname{arctg}(1 - \sqrt{3}) + \pi k$$

$$Au^2 + Bu^1v^1 + Cv^2 = 0$$

Однородное - это когда степень всех слагаемых одинаковая, а справа ноль

$$Au^2/v^2 + Bu^1/v^1 + C = 0$$

$$u/v = t$$

$$At^2 + Bt + C = 0$$

Ответ: $\operatorname{arctg}(1 + \sqrt{3}) + \pi k; \operatorname{arctg}(1 - \sqrt{3}) + \pi k$

$$\sin^3 3x - 4\sin^2 3x \cos 3x + 3\sin 3x \cos^2 3x = 0$$

$$\sin 3x = u$$

$$\cos 3x = v$$

Пусть $u=0 \Rightarrow v=0=0$

$$u^3 - 4u^2v + 3uv^2 = 0 | : u^3$$

$$u=0$$

$$\sin 3x = 0$$

$$3x = \pi n$$

$$x = \pi n / 3$$

$$1 - 4v/u + 3v^2/u^2 = 0$$

$$t = v/u$$

$$1 - 4t + 3t^2 = 0$$

$$t_1 = 1$$

$$t_2 = 1/3$$

$$\cos 3x / \sin 3x = 1$$

$$\operatorname{ctg} 3x = 1$$

$$3x = \pi/4 + \pi k$$

$$x = \pi/12 + \pi k/3$$

$$\operatorname{ctg} 3x = 1/3$$

$$3x = \operatorname{arctg}(1/3) + \pi k$$

$$x = \operatorname{arctg}(1/3)/3 + \pi k/3$$

Ответ: $\pi/12 + \pi k/3; \operatorname{arctg}(1/3)/3 + \pi k/3; \pi n/3$

$$(2\sin x \cos x - \cos^2 x) / (2\cos x - \sin x) = 0$$

$$2\sin x \cos x - \cos^2 x = 0$$

$$\sin x = v$$

$$\cos x = u$$

$$2vu - u^2 = 0$$

$$2v/u - 1 = 0$$

$$v/u = t$$

$$2t - 1 = 0$$

$$2t = 1$$

$$t = 1/2$$

$$\sin x / \cos x = 1/2$$

$$\operatorname{tg} x = 1/2$$

$$x = \operatorname{arctg}(1/2) + \pi k$$

Ответ: $\operatorname{arctg}(1/2) + \pi k; \pi/2 + \pi n$

$$2\cos x - \sin x = 0$$

$$2\cos x = \sin x$$

$$\sin x / 2\cos x = 1$$

$$\sin x / \cos x = 2$$

$$\operatorname{tg} x = 2$$

$$x = \operatorname{arctg}(2) + \pi k$$

Пусть $u=0 \Rightarrow 2vu - u^2 = 0$

$$\Rightarrow 0 = 0$$

$$\cos x = 0$$

$$x = \pi/2 + \pi n$$